Sequence Database Search

CS 4390/5390 Fall 2019

The (Sequence) Database Search Problem

Given a database *D* of sequences (DNA, Protein, Books, Web Pages) and a query string *Q* find the sting(s) *S* in *D* which is/are closest matches to *Q* under a defined scoring function.

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Scoring functions are typically either

- •Semi-global alignment -- The best possible alignment score between a substring A of S and Q, or
- Local alignment -- The vest possible alignment score between a substring A of S and a substring B of Q.

Evaluating Database Search

Sensitivity -- Ratio of true positives (substrings in the database matching the query string) found by the algorithm to the true number of positives.

Efficiency -- Running time of the method.

Types of Algorithms

Exhaustive Search -- Enumerate all possible solutions to find the best one. very sensitive, very slow

Heuristic Search -- Reduce the search space by estimating alignments but sometimes overlooks solutions. *less sensitive, fast*

Filter Based -- Select candidate positions in the database where the query is likely to match. *medium sensitivity, moderately fast*

Smith-Waterman's Revenge

For each sequence S in D, run Smith-Waterman between S and Q

Return the sequence(s) with the largest alignment score.

Running time is O(mn) per sequence, this is very slow, but very accurate.

FastP and FastA

The first attempts at speeding up search.

Both are based on the idea that (in protein sequences) replacements are more common than indels.

Developed in 1983 and 1988 respectively, FastP does not allow for gaps at all while FastA will find gapped alignments, but only in certain circumstances.

Step 1: Identify "hotspots" -- find *k*-mers that are shared between the query and the database using a lookup table (this table is 4^k for DNA and RNA, 20^k for Proteins)

Query

CAACTTGCC

Database ACGGTTACGTAGGTCCG

GCGTAGGCAGAAGTTGCCTGCGT

ACGAAGTAGCCGTCAGTC

Step 2: locating diagonal runs -- pairs (or larger groups) of hot spots such that the distance between the hot-spots is the same in both the query and the database sequence

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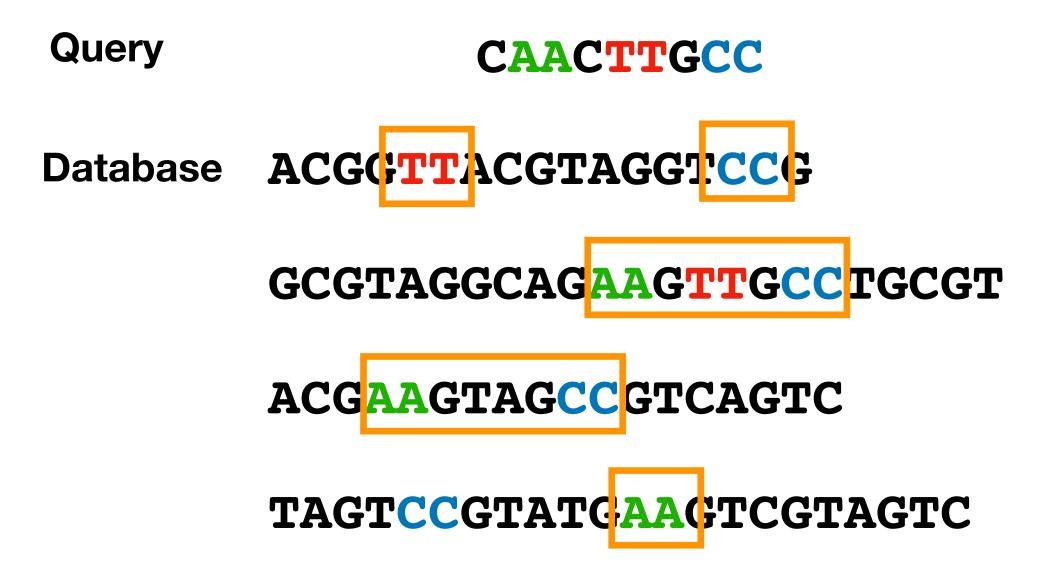
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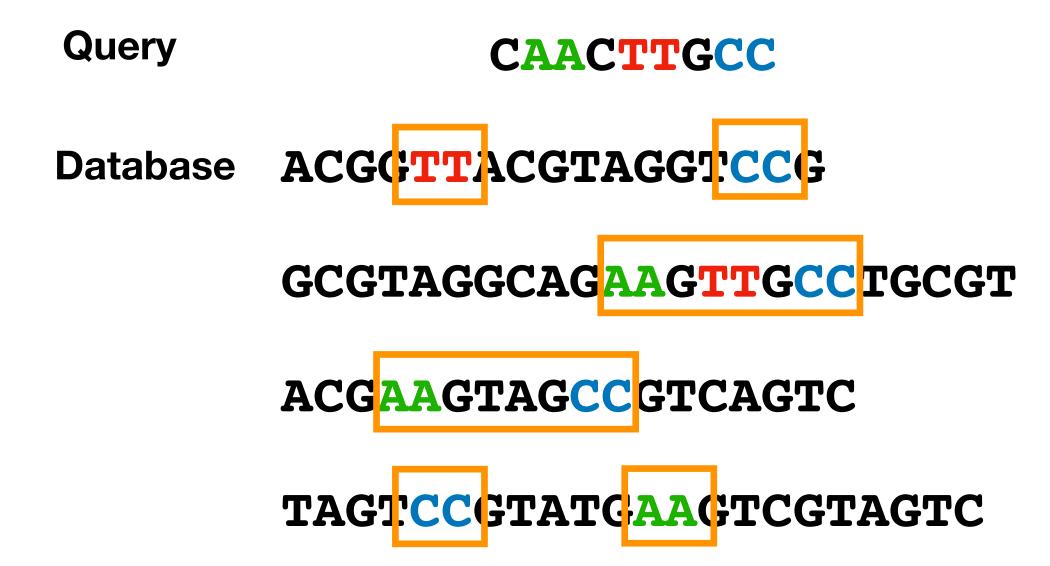
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CRACTTGCC

GCGTAGGCAGTCGCGTAGGCC

CRACTTGCC

GCGTAGGCAGTCGCGTAGGCC

CRACTTGCC

GCGTAGGCAGTCGCGTAGGCC

CRACTTGCC

GCGTAGGCAGTCGCGTAGGCC

CRACTTGCC

GCGTAGGCAGAAGTTGCCTAGGCC

CRACTTGCC

CRACTTGCC

GCGTAGGCAGAAGTTGCCTAGGCC

CRACTTGCC

CRACTTGCC

GCGTAGGCAGAAGTTGCCTAGGCC

CRACTTGCC

CRACTTGCC

GCGTAGGCC

CRACTTGCC

CRACTTGCC

GCGTAGGCC

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GCGTAGGCC

CRACTTGCC

CRACTTGCC

CRACTTGCC

GCGTAGGCC

CRACTTGCC

CRACTTGCC

CRACTTGCC

GCGTAGGCC

CRACTTGCC

CRACTTGCC

GCGTAGGCC

CRACTTGCC

CRACTTCC

CRACTTCC

CRACTTCC

CRACTTCC

CRACTTCC

CRACTTCC

CRACTT

The score of a diagonal run is the sum of the base-scores of the hotspots and penalties for inter-spot characters

Step 3: re-score the best diagonal runs -- rather than fixed inter-spot scores based on length, rescore the alignments using actual character matches

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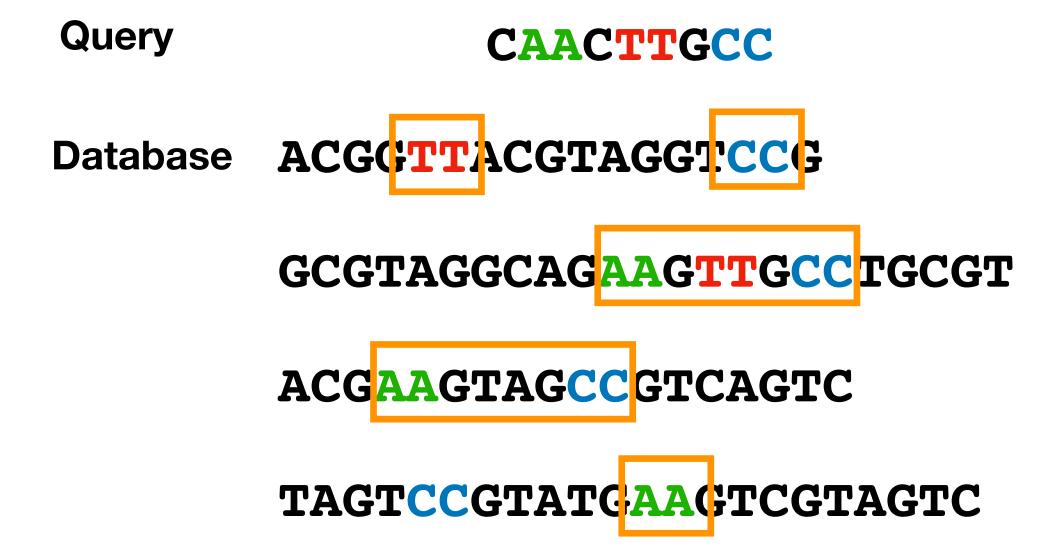
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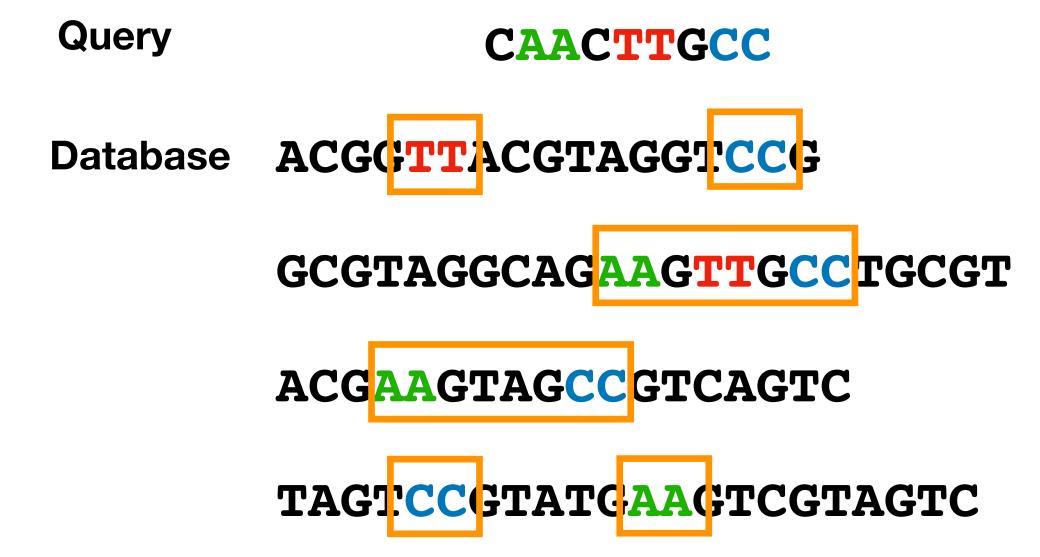
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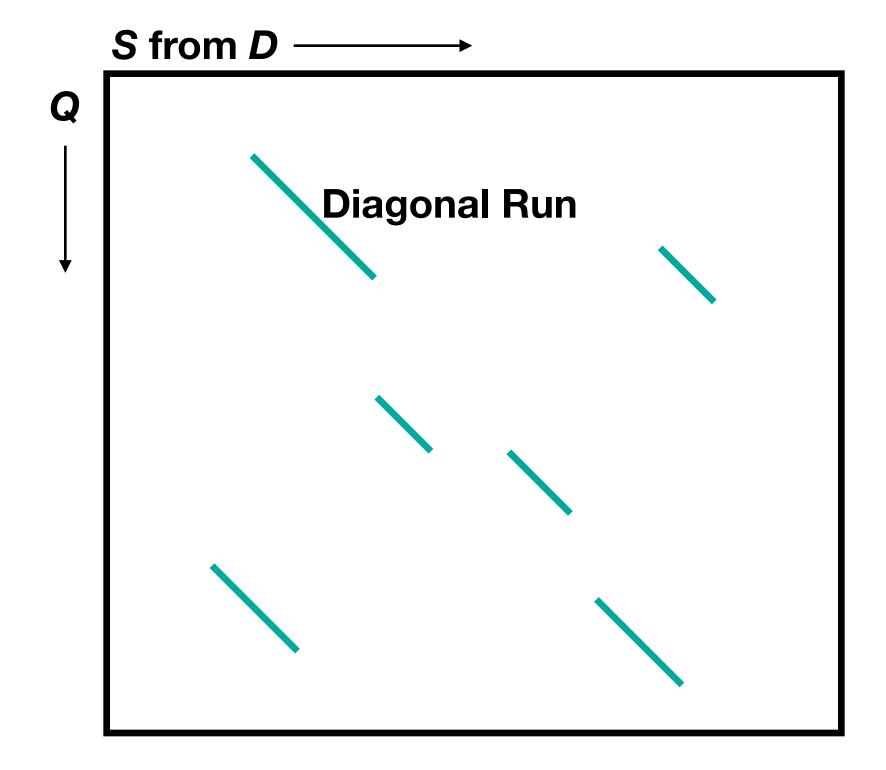
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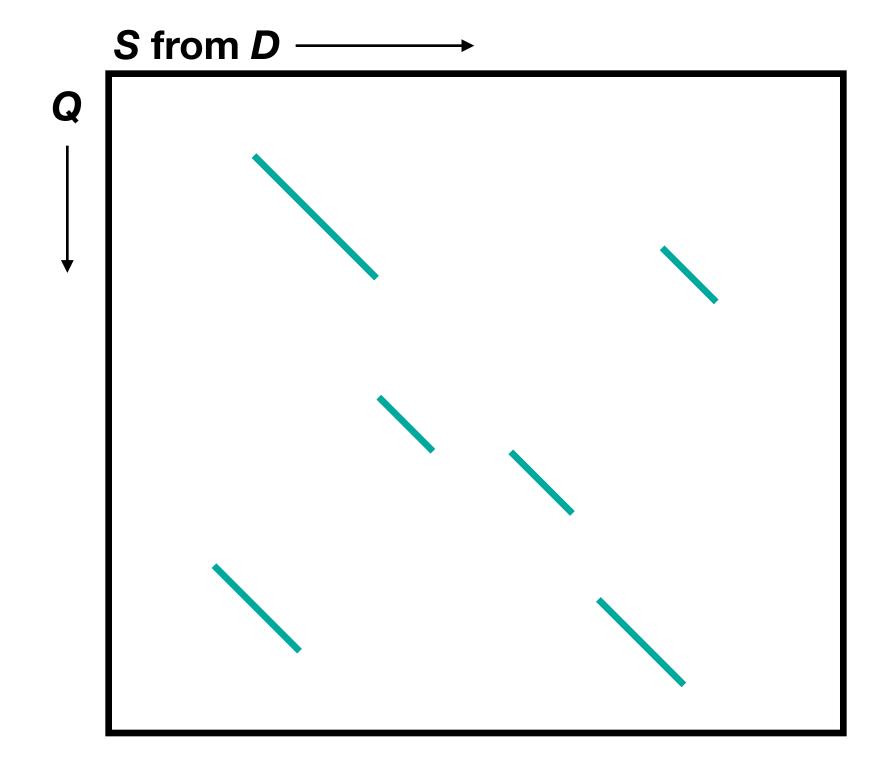
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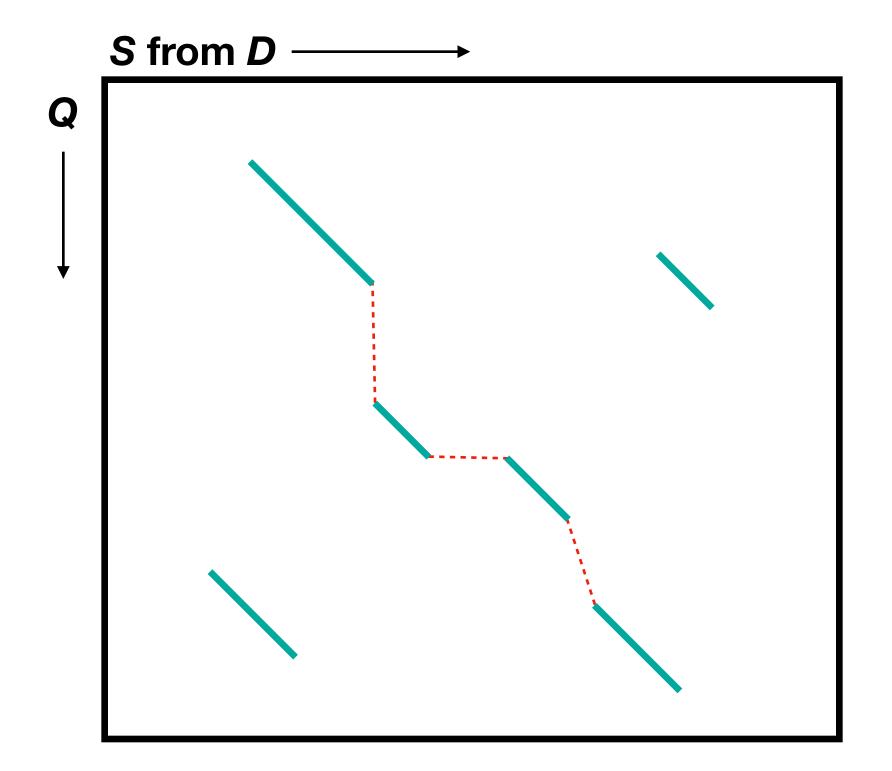
Step 4: join diagonal runs -- using a fixed score based on the locations of the regions, join them with a fixed gap-style cost

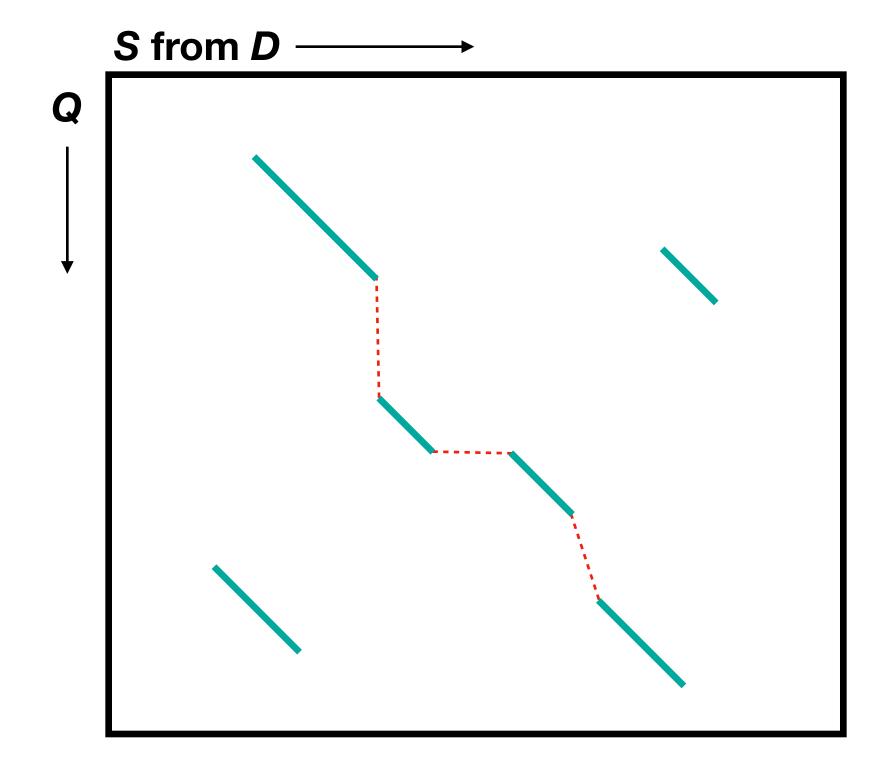


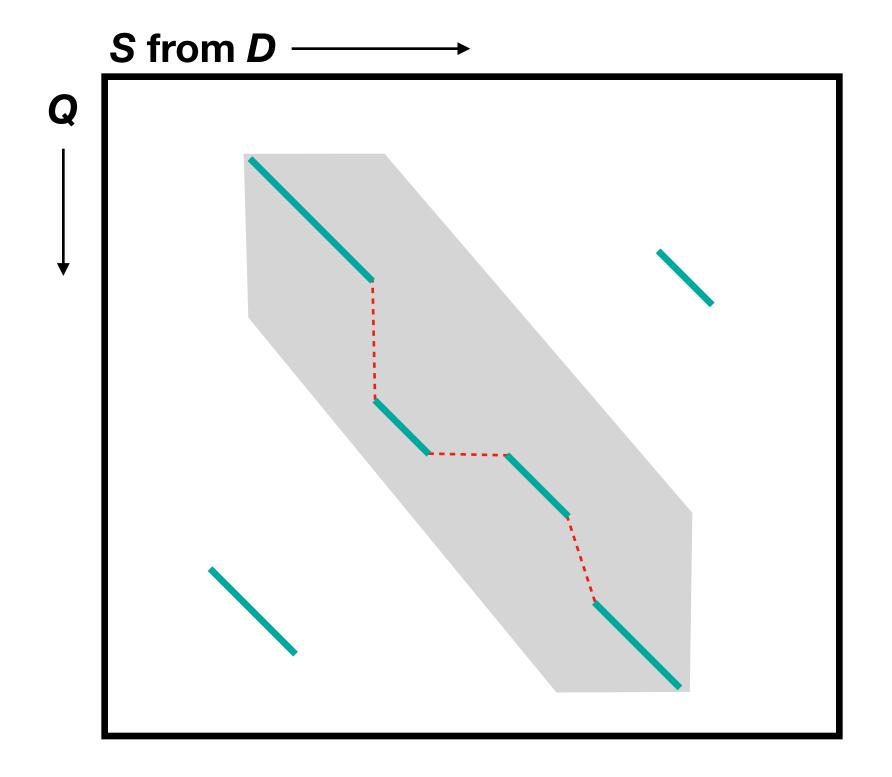
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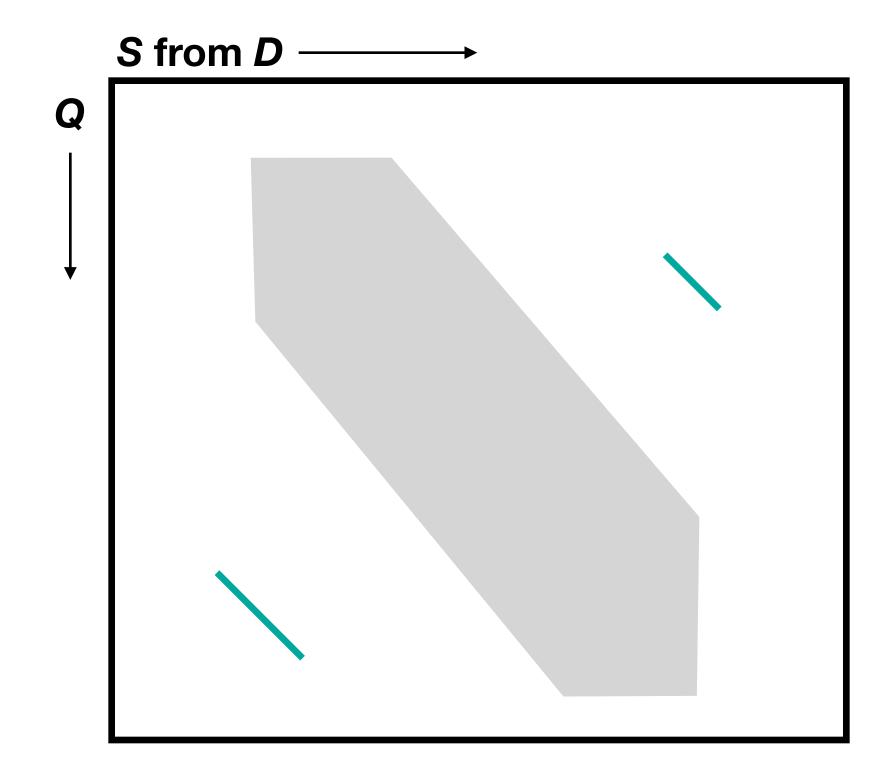


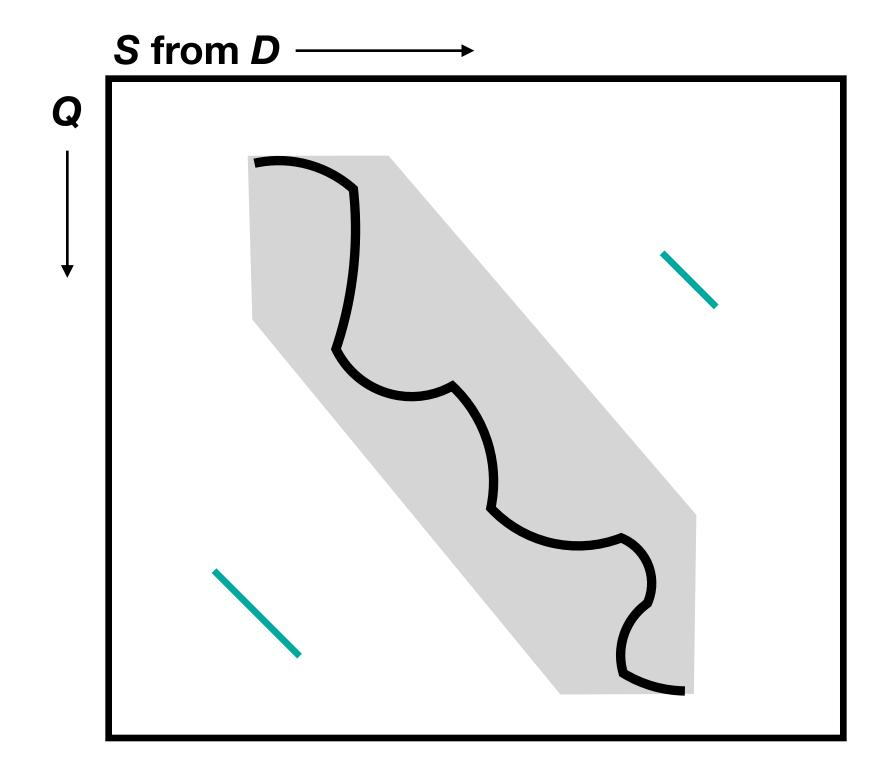
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Most commonly used database search tool in computational biology.

Originally published in 1990 by Altschul, Gish, Myers, Miller and Lipman.

Faster than FastA.

Step 1: Query-preprocessing:

- 1. split the query into *k*-mers
- 2. create a set of *neighbors* of each k-mer, other k-mers such that the replacement scores are not too high (this can be done with a Σ^k lookup table)

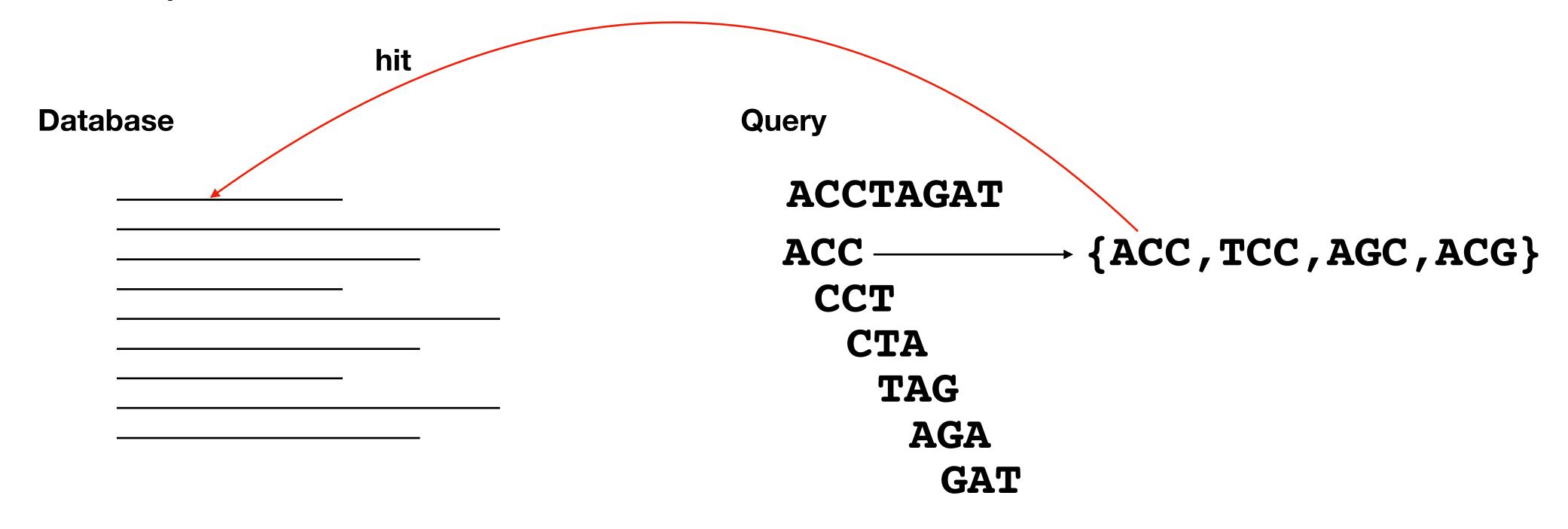
```
ACCTAGAT
ACC
CCT
CTA
TAG
AGA
GAT
```

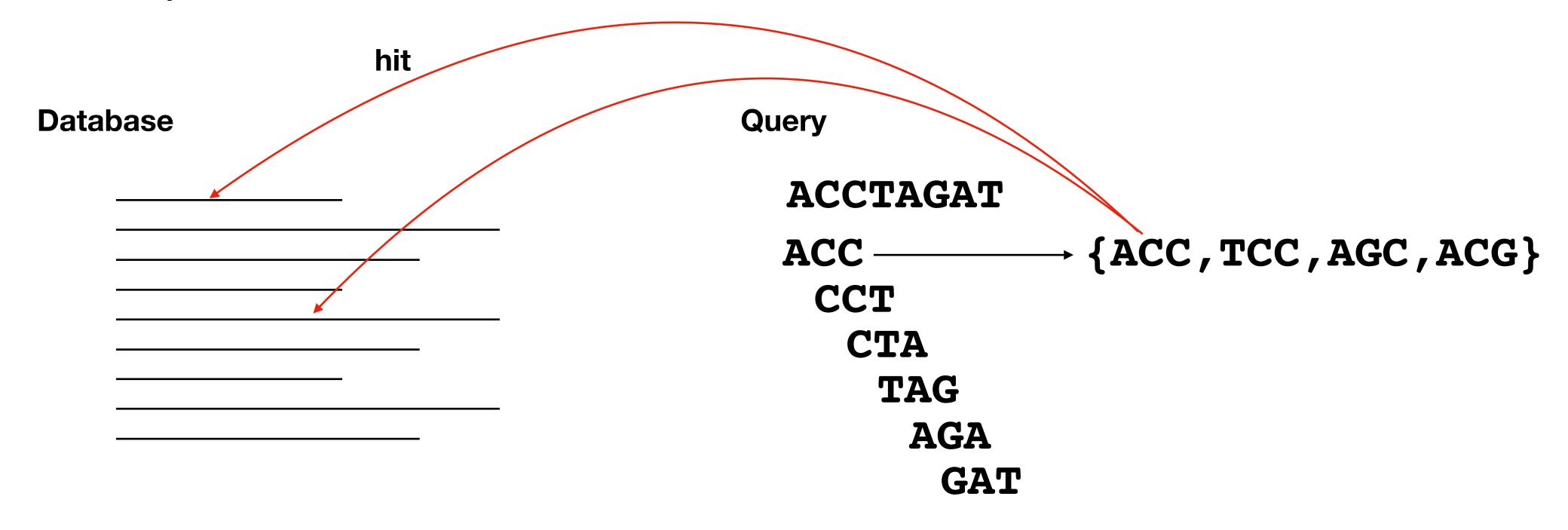
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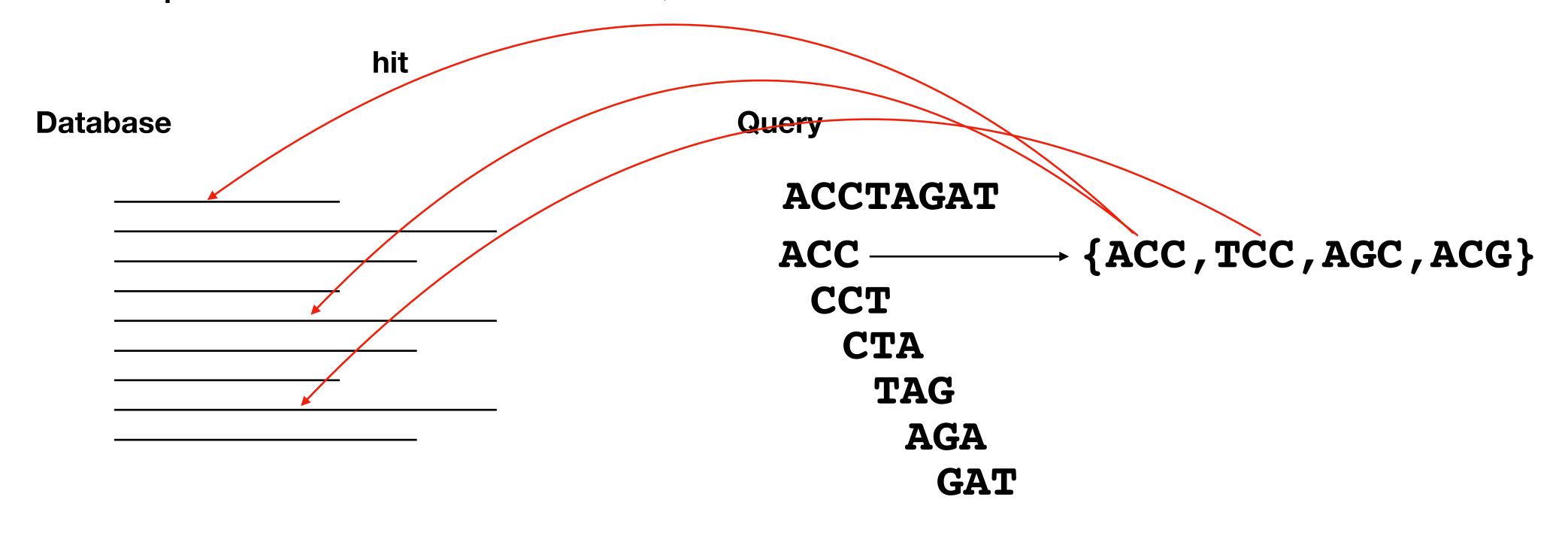
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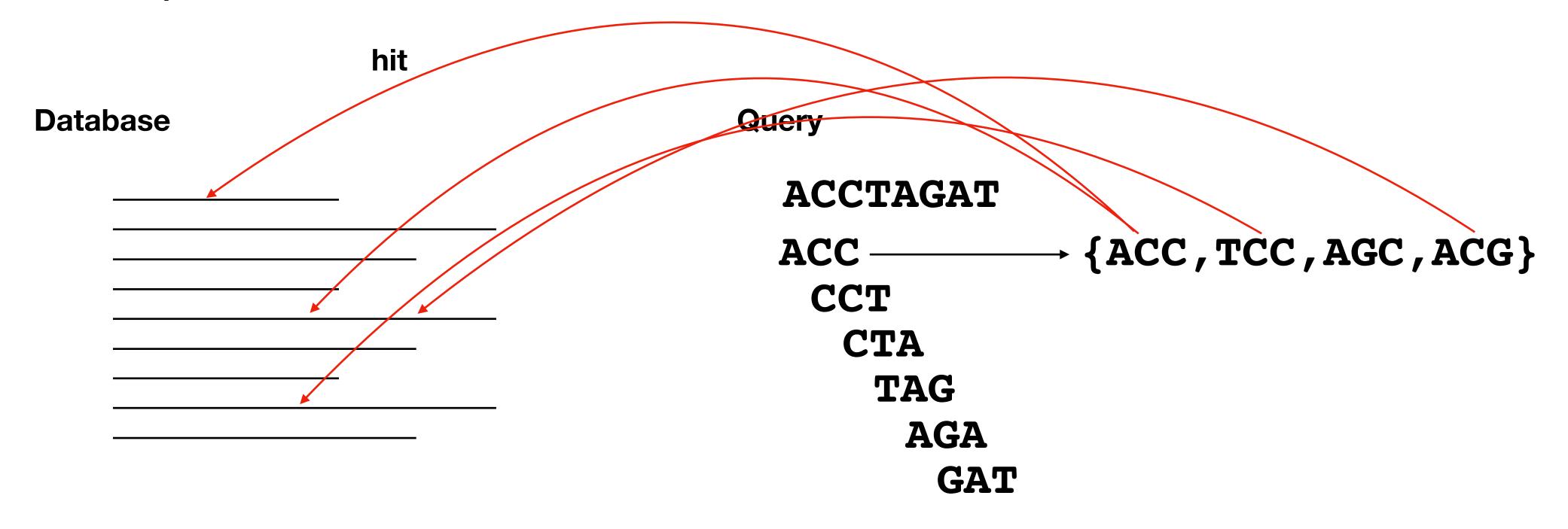
Step 2: Database scanning -- label any instance of a neighbor of Q in any sequence S of D as a "hit", collect all of these hits

Database	Query	
	ACCTAGAT	
	$ACC \longrightarrow \{ACC, TCC, AGC, PCC, PCC, PCC, PCC, PCC, PCC, PCC, P$	\CG}
	CCT	
	CTA	
	TAG	
	AGA	
	GAT	

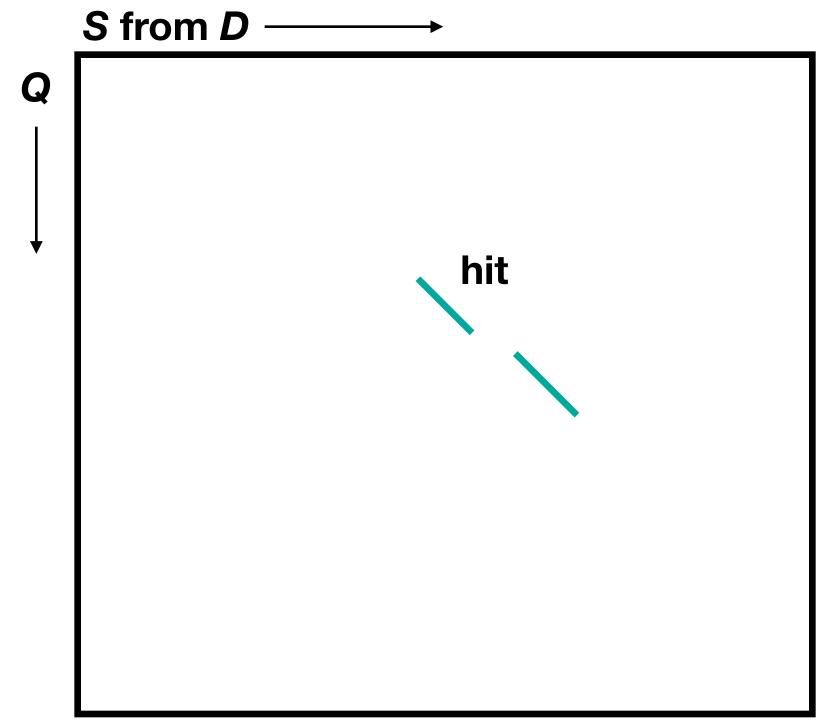




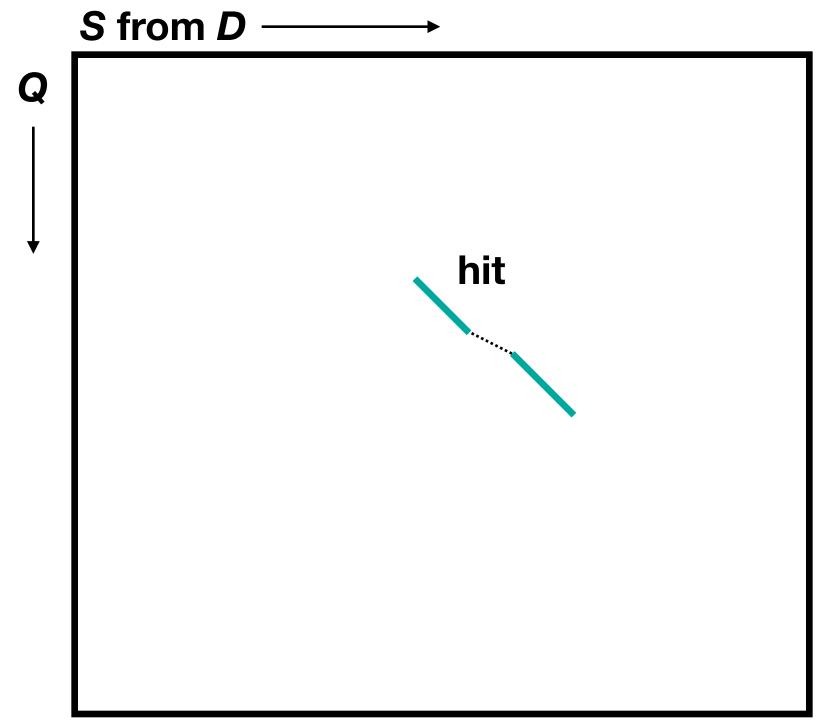




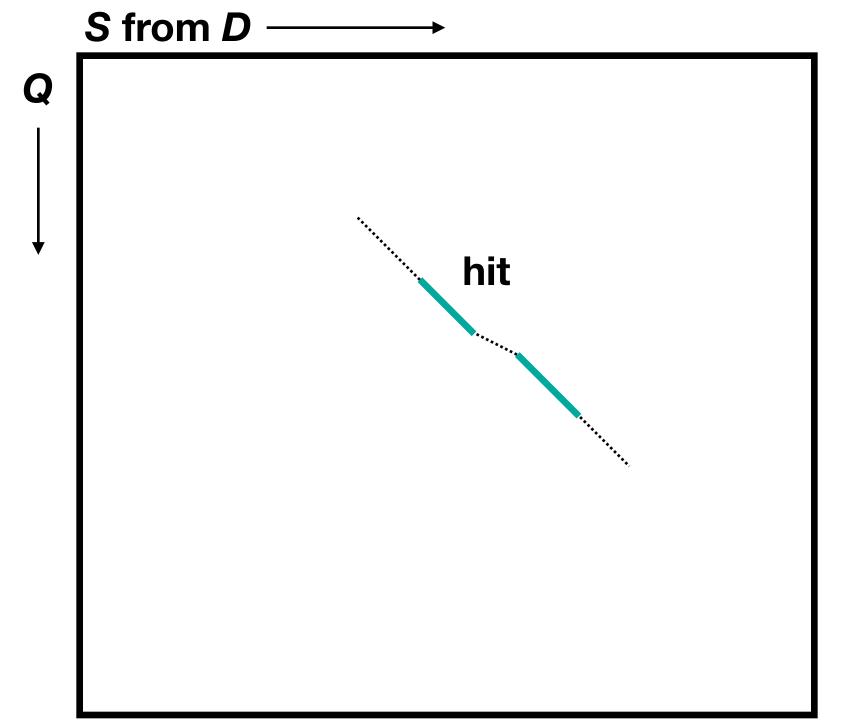
Step 3: Hit extension -- for any sequence S in D, with two hits (for protein, one for DNA) extend in either direction without gaps until the score drops too low



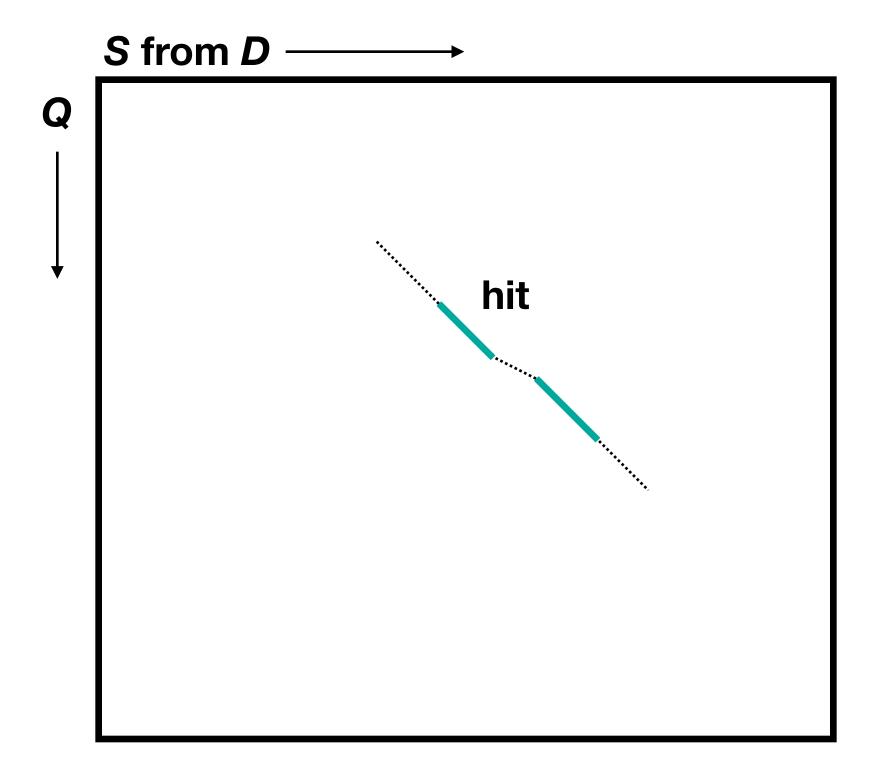
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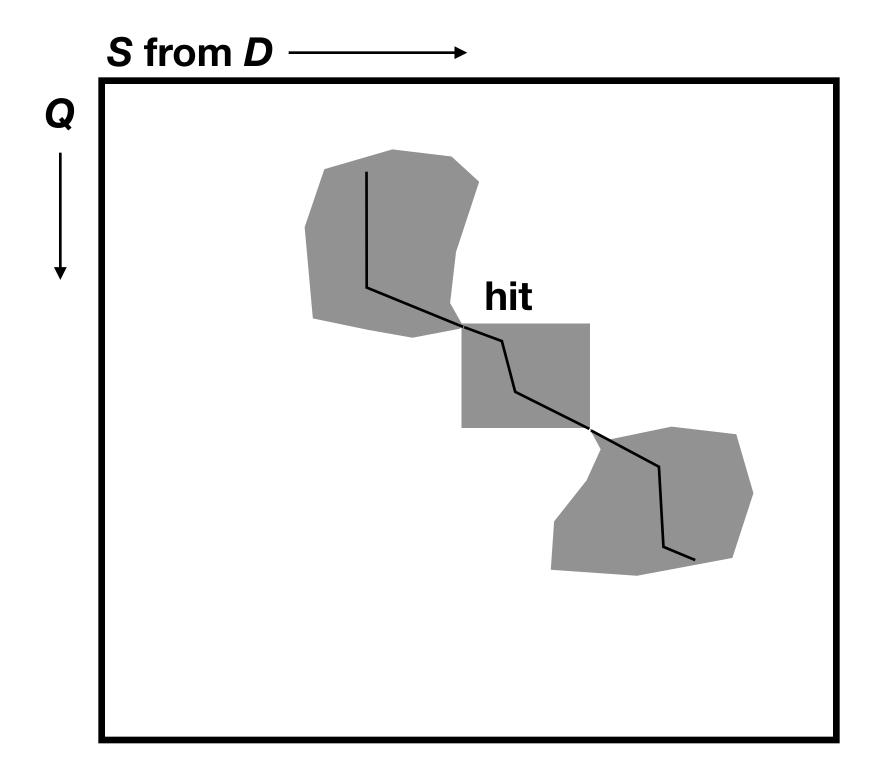
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• **E-value** is the expected number of alignments having an alignment score > S at random.

$$E = Kmne^{-\lambda S}$$

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- as the lengths double, the number of sequences with that score does
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- You can calculate *p-values* from the *E-value* is 1-e-E.

MegaBLAST

Greedy adaptation that only works for DNA

Takes in multiple query sequences rather than one

- concatenates the sequences together
- runs the query on this longer sequences
- results are resorted after

Uses linear (affine) gap costs by default

BLAST-Like Alignment Tool (BLAT)

Only works for DNA (not Protein or RNA)

Instead of creating a lookup table for the query, create one for the database

- this takes a lot of memory to store
- only store non-overlapping k-mers

Still uses a 2-hit requirement

Stitches together local alignments on the same database sequence to create larger alignments (think intron splicing)

PatternHunter

Only works on DNA

Uses a patented concept called Spaced Seeds

A spaced seed is a binary sequence BS has two parameters:

- weight, w, and
- length, m.
- It contains w 1's, and (m-w) 0's

Two sequences sequences of length *m* are a match if the characters at the positions of *BS* that are 1's match

Spaced seeds reduce the number of false matches

PatternHunter

```
111010010100110111
ACTCCGATATGCGGTAAC
|||-|--|-||-|||
ACTTCACTGTGAGGCAAC
```

```
111010010100110111

ACTCCAATATGCGGTAAC

| | | - | - - | - | - | | |

ACTCCAATATGCAGTAAC
```

```
1111111111
1111111111
```

```
111010010100110111
111010010100110111
```

PatternHunter

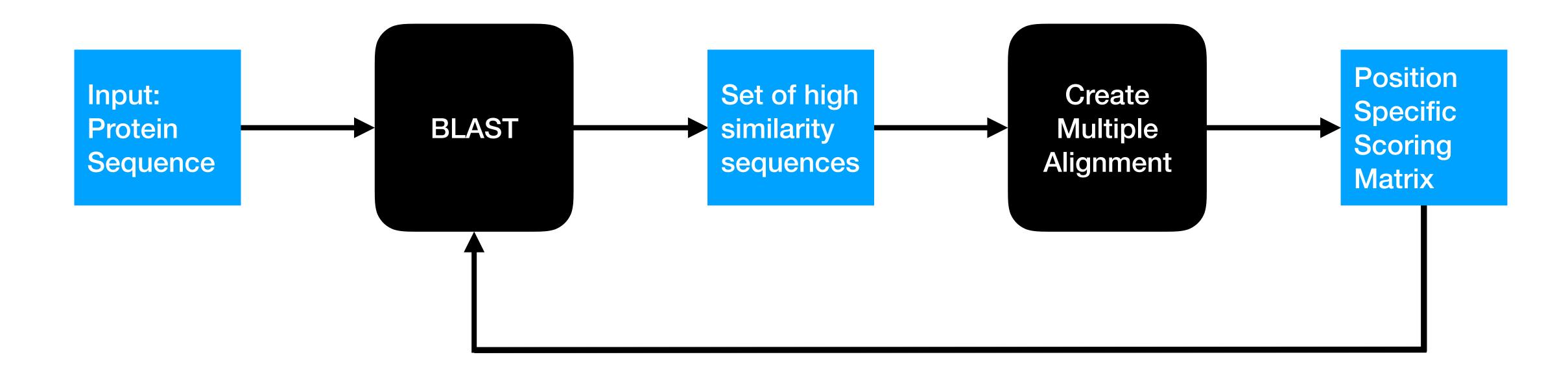
Lemma The expected number of hits of a weight-w length-m seed model within a length L region with similarity p ($p \in [0,1]$) is $(L-m+1)p^w$.

Proof For each possible position within the region, the probability of having w specific matches is p^w . Since there are L-m+1 possible positgions within the region, the expected number of hits is $(L-m+1)p^w$.

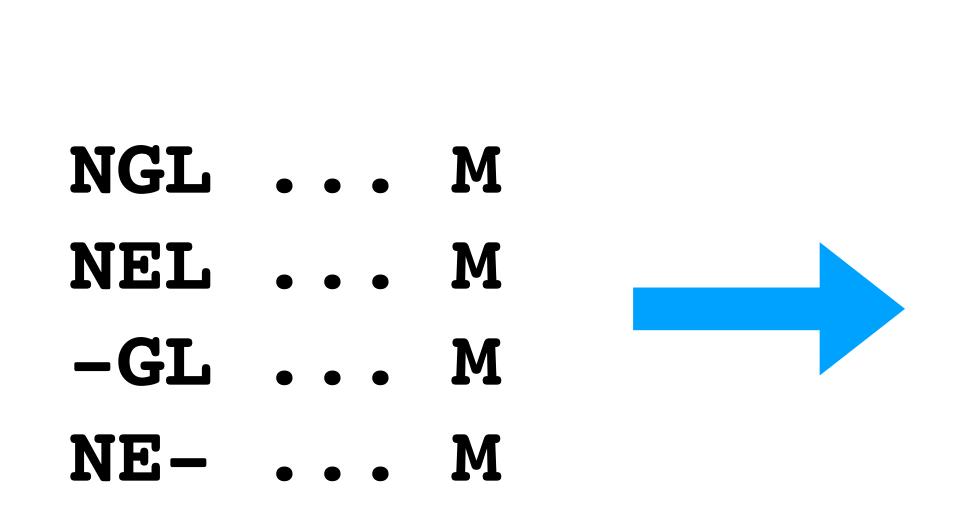
Example, a region of 64 characters, with 70% similarity. BLAST is expected to have 1.07 hits, and PatternHunter would have 0.93. (w=11, m=11 for BLAST, m=18 for PatternHunter)

Position-Specific Iterated BLAST (PSI-BLAST)

Designed to find distant protein sequences.



Position-Specific Iterated BLAST (PSI-BLAST)



Position	1	2	3		n
A	0	0	0		0
R	0	0	0	•••	0
N	100	0	0	•••	0
D	0	0	0	•••	0
C	0	0	0	•••	0
W	0	0	0		0
E	0	50	0	•••	0
G	0	50	0		0
H	0	0	0		0
	0	0	0		0
L	0	0	100		0
K	0	0	0		0
M	0	0	0	•••	100
F	0	0	0	•••	0
Р	0	0	0	•••	0
S	0	0	0	•••	0
T	0	0	0	•••	0
W	0	0	0	•••	0
Y	0	0	0		0
V	0	0	0	•••	0

Given

- a database, D
- a query, S
- a maximum difference, k, and
- the window size, w

Find:

- a set of (X, Y) where X and Y are length-w substrings in D and S respectively,
- such that the edit distance between X and Y is at most k.

Based on splitting the windows into q-grams (k-mers)

Lemma Given two length w sequences X and Y, if their edit distance is at most k, then they must share at least w+1-(k+1)q common q-grams.

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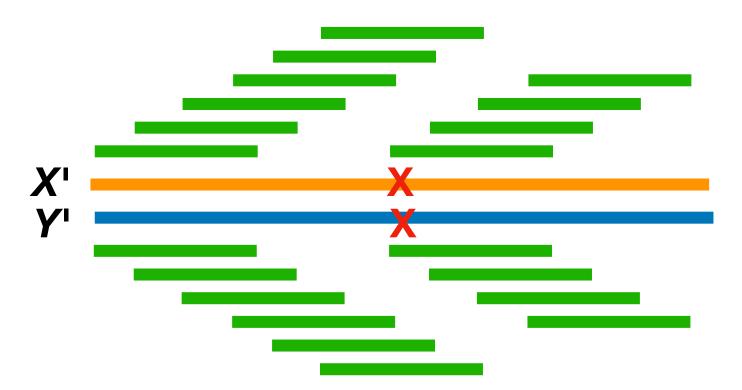
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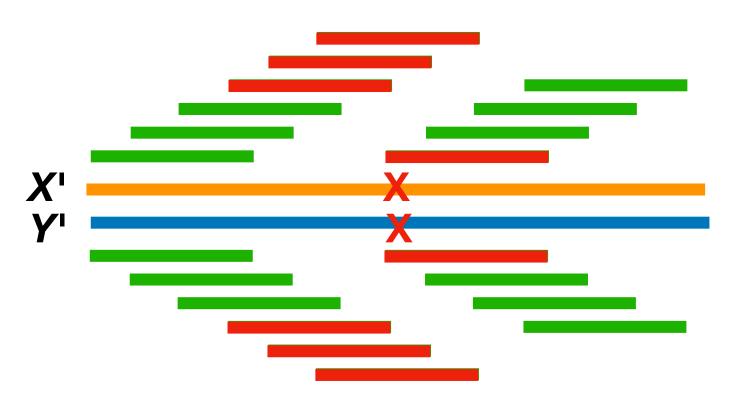
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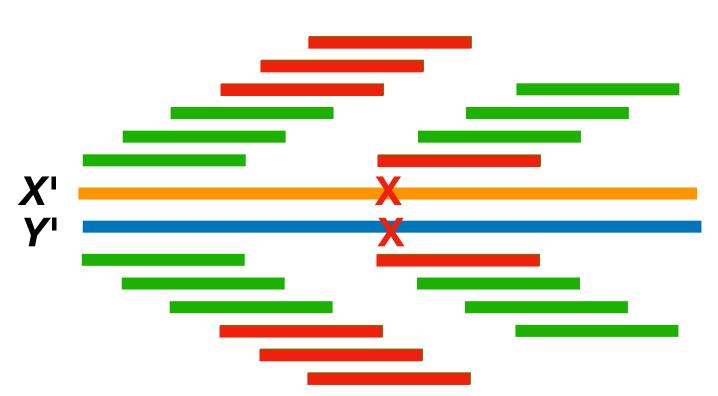
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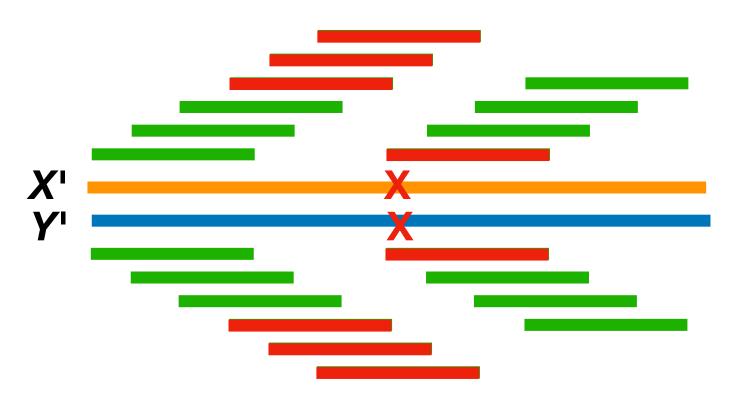
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- •Any common *q*-gram for *X*' and *Y*' is also common for *X* and *Y*.



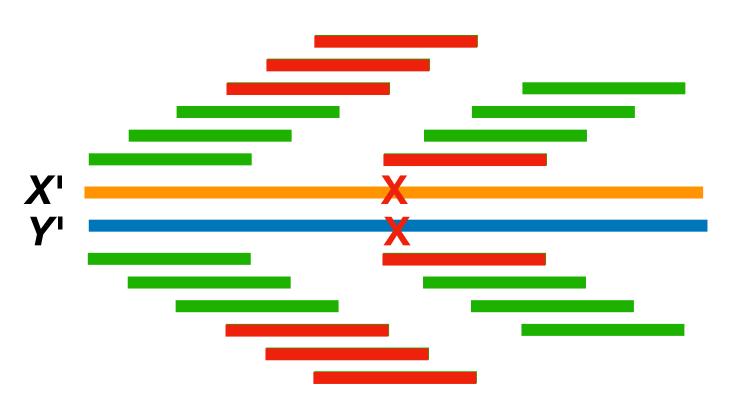
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This is just an application of the pigeon-hole principle



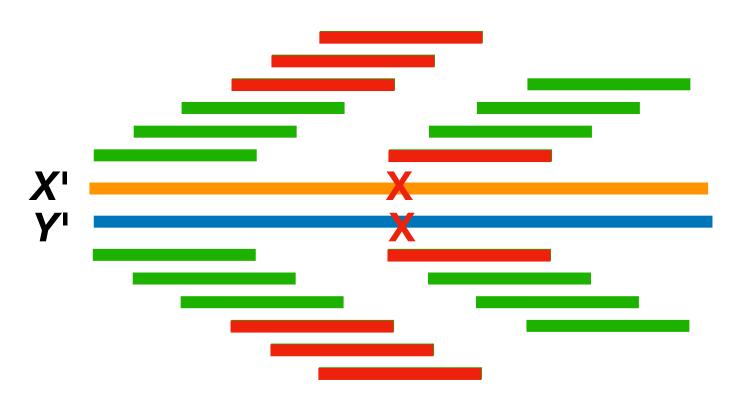
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If w+1-(k-1)q q-grams match, can edit distance be higher than k?

The actual QUASAR algorithm uses this principle to find potential alignments:

- for each w length substring of S, X and
 - maintain counters for each w length substring of D, Y
 - for each q-gram in S, increment the counters for the Y that contain it
 - for all Y with counter greater than w+1-(k+1)q, run a sequence alignment algorithm

The actual QUASAR algorithm uses this principle to find potential alignments:

- for each w length substring of S, X and
 - maintain counters for each w length substring of D, Y
 - for each q-gram in S, increment the counters for the Y that contain it
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- When searching for the q-grams in D
- along with an additional array idx(Q) which points to the begining of the locations that start with Q in the suffix array.

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i	SA[i]		
1	5	ACT	idx(AC)
2	2	AGCT	idx(AG)
3	4	CACT	idx(CA)
4	1	CAGCACT	
5	6	СТ	idx(CT)
6	3	GCACT	idx(GC)
7	7	${f T}$	

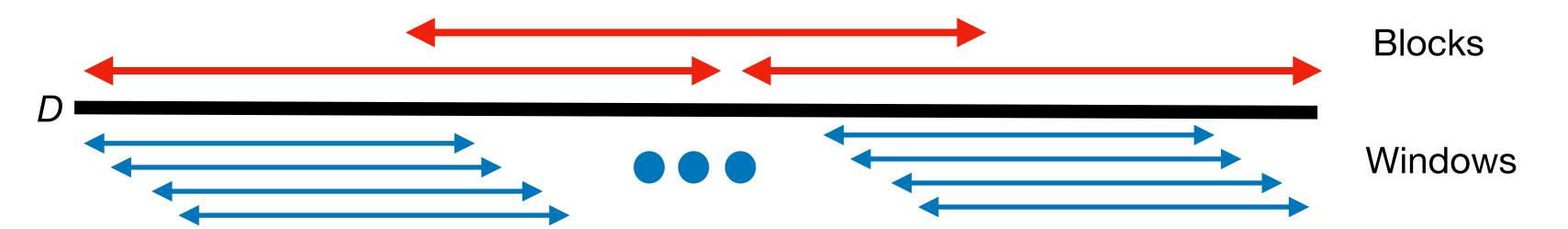
Speedups

Window Shifting

•Similar to the solution to homework 2, each window shared quite a few q-grams with the one before it, use that to reduce running time.

Block Addressing

- •Rather than counting the occurrences in all Y, break D into non-overlapping blocks of b (> 2w) and keep counters there
- Keep a second offset set of blocks to not miss any spanning windows.
- If any block contains enough matching q-grams, run a more detailed pass



Running time

• Suffix array construction $O(|D| \log |D|)$

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Total search time is
$$O\left(\frac{|S||D|}{4q} + cb^2\right)$$

Space

• Suffix array takes $O(|D| \log |D|)$ space, then $O(|D|/b + b^2)$ space for the query.

Locality Sensitive Hashing

The idea of locality sensitive hashes, is that you can use an efficient to compute hash to estimate something that is computationally difficult.

Let s be the similarity you would like to estimate, and h be a hash function on the same types of elements. (d would take two arguments and return a distance, h takes one argument and returns something).

We say h is an LSH for d if

 $\bullet s(x,y) = pr(h(x)=h(y))$

We say h is a gapped LSH for d if the following holds:

- if $s(x,y) \le s_1$ then $pr(h(x)=h(y)) \le p_1$, and
- if $s(x,y) \ge s_2$ then $pr(h(x)=h(y)) \ge p_2$.
- more precisely it's (s₁,s₂,p₁,p₂)-sensitive.

Quick digression to Hamming Distance

We know edit distance is the minimum number of insertions, deletions, and mismatches to convert one string into another.

Hamming distance is the minimum number of only mismatches.

Also used in vectors, the number of dimensions that have different values.

Locality Sensitive Hashing

Let $h_{k,\pi}(s)$ be a function that takes string s and return a selected set of k characters based on some random ordering of integers π .

If the hamming distance of s_1 and s_2 , both of length w, is d, then

$$Pr\left(h_{k,\pi}(s_1) = h_{k,\pi}(s_2)\right) = \prod_{j=1,\dots,k} Pr\left(s_1\left[\pi\left[j\right]\right] = s_2\left[\pi\left[j\right]\right]\right) = \left(1 - \frac{d}{w}\right)^k$$

In other words, the more similar the sequences are (the lower *d* is and thus) the higher probability of a hash collision.

Using the Locality Sensitive Hash described for hamming distance, locate highly-probable match locations.

The LSH can introduce false discoveries:

- False positive: s_1 and s_2 are dissimilar, but $h_{k,\pi}(s_1) = h_{k,\pi}(s_2)$
 - -can be eliminated by checking the actual hamming distance
- False negative: s_1 and s_2 are similar, but $h_{k,\pi}(s_1) \neq h_{k,\pi}(s_2)$
 - -can be reduced by repeating search using multiple π

Algorithm (given Q, D, w, d, m)

- generate m random orderings π_1 , π_2 ,..., π_m .
- for every w-mer s in D, compute $h_{k,\pi 1}(s)$, $h_{k,\pi m}(s)$, ..., $h_{k,\pi m}(s)$.
- for every pair of w-mers s and t from D and Q such that $h_{k,\pi j}(s) = h_{k,\pi j}(t)$ for some j
 - if the hamming distance between s and t is less than d, report (s,t)

$$\prod_{1 \le i \le m} \left(1 - Pr\left(h_{k,\pi_i} \left(s_1 \right) = h_{k,\pi_i} \left(s_2 \right) \right) \right)$$

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Remember that
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Are the methods presented good enough?

8,000 queries

- 2,000 from each of 4 species: chimpanzee, mouse, chicken, zebrafish
- length ranged from 170-19,000 bases (average of 2,700)

Aligned to the human genome using BLAST

Baseline is an exact search algorithm called BWT-SW (not discussed in class, but in the posted book chapter if interested)

<i>E</i> -Value	Percentage of	missing			
<u> </u>	Chimpanzee	Mouse	Chicken	Zebrafish	All Four Species
10^{-16}	0.00	0.03	0.05	0.06	0.01
10^{-15}	0.00	0.03	0.05	0.06	0.02
10^{-14}	0.00	0.04	0.06	0.06	0.02
10^{-13}	0.00	0.03	0.07	0.14	0.02
10^{-12}	0.01	0.04	0.10	0.17	0.03
10^{-11}	0.02	0.05	0.11	0.28	0.05
10^{-10}	0.02	0.07	0.13	0.39	0.06
10^{-9}	0.03	0.09	0.16	0.60	0.08
10^{-8}	0.05	0.11	0.25	0.77	0.12
10^{-7}	0.10	0.19	0.31	0.81	0.18
10^{-6}	0.17	0.31	0.45	1.08	0.28
10^{-5}	0.32	0.47	0.70	1.45	0.45
10^{-4}	0.57	0.88	0.99	1.81	0.75
10^{-3}	0.99	1.36	1.25	2.25	1.17
10^{-2}	1.69	2.11	1.68	2.61	1.84
10^{-1}	2.70	2.97	2.33	2.86	2.76

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Usually considered a "significant match"

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Protein Replacement Matricies

To now we have been talking about a "score" between two sequences without gaps with the penalties in the abstract.

Most people will use one of the *PAM* (percent accepted mutations), *BLOSUM* (blocks substitution matrix), *or VTML* series of replacement (or transition) matrices.

All 3 are based on statistics from databases of proteins labeled in order to match based on function.

Protein Replacement Matrices

BLOSUM (most popular) published by Henikoff & Henikoff in 1992.

Usually accompanied by a number (i.e. BLOSUM62, on the right) which is the percent identity of the pairs of sequences used for training.

The actual value is a log-odds value of the replacements from a large set of examples.

```
V 0 -3 -3 -3 -1 -2 -2 -3 -3 3 1 -2 1 -1 -2 -2 0 -3 -1 4
```

Protein Replacement Matrices

PAM and VTML also have numbers associated, but the allowable amount of time between sequences¹, so its inversely correlated with the BLOSUM number.

Somewhat equivalent matrices (by entropy)

BLOSUM90	PAM100	VTML100
BLOSUM80	PAM120	VTML120
BLOSUM60	PAM160	VTML160
BLOSUM52	PAM200	VTML200
BLOSUM45	PAM250	VTML250

¹Time is measured relative to the evolutionary time it takes to introduce one change per 100 amino acids.

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

```
S 1 -1 1 0 -1 0 0 0 -1 -2 -2 0 -1 -2 -1 4
T 0 -1 0 -1 -1 -1 -1 -2 -2 -1 -1 -1 -1 -2 -1 1 5
W -3 -3 -4 -4 -2 -2 -3 -2 -2 -3 -2 -3 -1 1 -4 -3 -2 11
Y -2 -2 -2 -3 -2 -1 -2 -3 2 -1 -1 -2 -1 3 -3 -2 -2 2 7
V 0 -3 -3 -3 -1 -2 -2 -3 -3 3 1 -2 1 -1 -2 -2 0 -3 -1 4
```

P

Given the sequence **VPNM**, a threshold of 8, wand *k*-mer size 2 perform BLAST v preprocessing to find the set of *k*-mers to search for.

```
S 1 -1 1 0 -1 0 0 0 -1 -2 -2 0 -1 -2 -1 4
T 0 -1 0 -1 -1 -1 -1 -2 -2 -1 -1 -1 -1 -2 -1 1 5
W -3 -3 -4 -4 -2 -2 -3 -2 -2 -3 -2 -3 -1 1 -4 -3 -2 11
Y -2 -2 -2 -3 -2 -1 -2 -3 2 -1 -1 -2 -1 3 -3 -2 -2 2 7
V 0 -3 -3 -3 -1 -2 -2 -3 -3 3 1 -2 1 -1 -2 -2 0 -3 -1 4
```

P

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

```
S 1 -1 1 0 -1 0 0 0 -1 -2 -2 0 -1 -2 -1 4
T 0 -1 0 -1 -1 -1 -1 -2 -2 -1 -1 -1 -1 -2 -1 1 5
W -3 -3 -4 -4 -2 -2 -3 -2 -2 -3 -2 -3 -1 1 -4 -3 -2 11
Y -2 -2 -2 -3 -2 -1 -2 -3 2 -1 -1 -2 -1 3 -3 -2 -2 2 7
V 0 -3 -3 -3 -1 -2 -2 -3 -3 3 1 -2 1 -1 -2 -2 0 -3 -1 4
```

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	A	R	N	D	C	Q	E	G	Н	I	L	K	M	F	P	S	T	M	Y	V	X	
Α	4																					
R	-1	5																				
N	-2	0	6																			
D	-2	-2	1	6																		
C	0	-3	-3	-3	9											7.7	D					
Q	-1	1	0	0	-3	5										V						
E	-1	0	0	2	-4	2	5									V	P					
G	0	-2	0	-1	-3	-2	-2	6								4	+7	=	11			
H	-2	0	1	-1	-3	0	0	-2	8													
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4												
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4											
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5										
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5									
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6								
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7							
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4						
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5					
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11				
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7			
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4		
X	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	

P N M

P

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

```
= 11
                                    4+7
S 1 -1 1 0 -1 0 0 0 -1 -2 -2 0 -1 -2 -1 4
T 0 -1 0 -1 -1 -1 -1 -2 -2 -1 -1 -1 -1 -2 -1 1 5
W -3 -3 -4 -4 -2 -2 -3 -2 -2 -3 -2 -3 -1 1 -4 -3 -2 11
Y -2 -2 -2 -3 -2 -1 -2 -3 2 -1 -1 -2 -1 3 -3 -2 -2 2 7
V 0 -3 -3 -3 -1 -2 -2 -3 -3 3 1 -2 1 -1 -2 -2 0 -3 -1 4
```

V P N
V

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

```
0+7 = 7
S 1 -1 1 0 -1 0 0 0 -1 -2 -2 0 -1 -2 -1 4
T 0 -1 0 -1 -1 -1 -1 -2 -2 -1 -1 -1 -1 -2 -1 1 5
W -3 -3 -4 -4 -2 -2 -3 -2 -2 -3 -2 -3 -1 1 -4 -3 -2 11
Y -2 -2 -2 -3 -2 -1 -2 -3 2 -1 -1 -2 -1 3 -3 -2 -2 2 7
V 0 -3 -3 -3 -1 -2 -2 -3 -3 3 1 -2 1 -1 -2 -2 0 -3 -1 4
```

V P N
V

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

```
-3+7 = 4
S 1 -1 1 0 -1 0 0 0 -1 -2 -2 0 -1 -2 -1 4
T 0 -1 0 -1 -1 -1 -1 -2 -2 -1 -1 -1 -1 -2 -1 1 5
W -3 -3 -4 -4 -2 -2 -3 -2 -2 -3 -2 -3 -1 1 -4 -3 -2 11
Y -2 -2 -2 -3 -2 -1 -2 -3 2 -1 -1 -2 -1 3 -3 -2 -2 2 7
V 0 -3 -3 -3 -1 -2 -2 -3 -3 3 1 -2 1 -1 -2 -2 0 -3 -1 4
```

V P
V

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

	A	R	N	D	C	Q	E	G	Н	I	L	K	M	F	P	S	T	M	Y	V	X	
A	4																					
R	-1	5																				
N	-2	0	6																			
D	-2	-2	1	6																		
C	0	-3	-3	-3	9											77	Ъ					
Q	-1	1	0	0	-3	5										V						
E	-1	0	0	2	-4	2	5									I	P					
G	0	-2	0	-1	-3	-2	-2	6								3.	+7	=	10			
H	-2	0	1	-1	-3	0	0	-2	8													
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4												
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4											
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5										
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5									
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6								
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7							
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4						
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5					
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11				
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7			
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4		
Х	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	

V P
V P

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

	A	R	N	D	C	Q	E	G	Н	I	L	K	M	F	P	S	T	M	Y	V	X
A	4																				
R	-1	5																			
N	-2	0	6																		
D	-2	-2	1	6																	
C	0	-3	-3	-3	9											77	D				
Q	-1	1	0	0	-3	5										V	_				
E	-1	0	0	2	-4	2	5									I	P				
G	0	-2	0	-1	-3	-2	-2	6								3	+7	=	10		
Η	-2	0	1	-1	-3	0	0	-2	8												
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4											
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4										
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5									
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5								
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6							
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7						
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4					
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5				
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11			
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7		
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4	
Х	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1

V P N
V

VP IP

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

	A	R	N	D	C	Q	E	G	Н	I	L	K	M	F	P	S	T	M	Y	V	X
A	4																				
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D	-2	-2	1	6																	
C	0	-3	-3	-3	9											77	D				
Q	-1	1	0	0	-3	5										V	_				
E	-1	0	0	2	-4	2	5									L	P				
G	0	-2	0	-1	-3	-2	-2	6								1	+7	=	8		
Η	-2	0	1	-1	-3	0	0	-2	8												
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4											
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4										
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5									
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5								
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6							
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7						
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4					
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5				
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11			
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7		
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4	
Х	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1

V P N J

VP IP

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

	A	R	N	D	C	Q	E	G	H	I	L	K	M	F	P	S	T	M	Y	V	X	
A	4																					
R	-1	5																				
N	-2	0	6																			
D	-2	-2	1	6																		
C	0	-3	-3	-3	9											7.7	Ъ					
Q	-1	1	0	0	-3	5											P					
E	-1	0	0	2	-4	2	5									L	P					
G	0	-2	0	-1	-3	-2	-2	6								1	+7	=	8			
H	-2	0	1	-1	-3	0	0	-2	8													
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4												
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4											
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5										
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5									
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6								
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7							
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4						
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5					
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11				
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7			
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4		
Х	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	

V P N N

VP IP LP

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

	A	R	N	D	C	Q	E	G	Н	I	L	K	M	F	P	S	T	W	Y	V	X
A	4																				
R	-1	5																			
N	-2	0	6																		
D	-2	-2	1	6																	
С	0	-3	-3	-3	9											V	P				
Q	-1	1	0	0	-3	5										_	_				
E	-1	0	0	2	-4	2	5									M	P				
G	0	-2	0	-1	-3	-2	-2	6								1	+7	=	8		
H	-2	0	1	-1	-3	0	0	-2	8												
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4											
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4										
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5									
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5								
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6							
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7						
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4					
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5				
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11			
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7		
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4	
Х	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1

V P N N

VP IP LP

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

	A	R	N	D	C	Q	E	G	Н	I	L	K	M	F	P	S	T	M	Y	V	X	
A	4																					
R	-1	5																				
N	-2	0	6																			
D	-2	-2	1	6																		
C	0	-3	-3	-3	9											7.7	Ъ					
Q	-1	1	0	0	-3	5										V						
E	-1	0	0	2	-4	2	5									M	P					
G	0	-2	0	-1	-3	-2	-2	6								1.	+7	=	8			
H	-2	0	1	-1	-3	0	0	-2	8													
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4												
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4											
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5										
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5									
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6								
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7							
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4						
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5					
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11				
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7			
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4		
Х	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	

V P N N

VP IP LP MP

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

```
S 1 -1 1 0 -1 0 0 0 -1 -2 -2 0 -1 -2 -1 4
T 0 -1 0 -1 -1 -1 -1 -2 -2 -1 -1 -1 -1 -2 -1 1 5
W -3 -3 -4 -4 -2 -2 -3 -2 -2 -3 -2 -3 -1 1 -4 -3 -2 11
Y -2 -2 -2 -3 -2 -1 -2 -3 2 -1 -1 -2 -1 3 -3 -2 -2 2 7
V 0 -3 -3 -3 -1 -2 -2 -3 -3 3 1 -2 1 -1 -2 -2 0 -3 -1 4
```

V P N M

VP IP LP MP

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

	A	R	N	D	C	Q	E	G	Н	I	L	K	M	F	P	S	T	M	Y	V	X
A	4																				
R	-1	5																			
N	-2	0	6																		
D	-2	-2	1	6																	
С	0	-3	-3	-3	9																
Q	-1	1	0	0	-3	5															
E	-1	0	0	2	-4	2	5														
G	0	-2		-1	-3	-2	-2	6													
H	-2	0	1	-1	-3	0	0	-2	8												
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4											
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4										
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5									
Μ	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5								
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6							
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7						
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4					
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5				
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11			
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7		
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4	
Х	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1

V P N M
V P N

VP IP LP MP

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

	A	R	N	D	C	Q	E	G	H	I	L	K	M	F	P	S	T	M	Y	V	X
A	4																				
R	-1	5																			
N	-2	0	6																		
D	-2	-2	1	6																	
С	0	-3	-3	-3	9																
Q	-1	1	0	0	-3	5															
E	-1	0	0	2	-4	2	5														
G	0	-2	0	-1	-3	-2	-2	6													
H	-2	0	1	-1	-3	0	0	-2	8												
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4											
L	-1	-2	-3	-4	-1			-4	-3	2	4										
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5									
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5								
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6							
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7						
S	777	-1	125	10025	827	0	100.00	- 30	1000		100	7.7	100	27/22	- 972						
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5				
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11			
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7		
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4	
Χ	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1

N I	M
N	

VP IP LP MP

PN

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

	A	R	N	D	C	Q	E	G	Н	I	L	K	M	F	P	S	T	W	Y	V	X
Α	4																				
R	-1	5																			
N	-2	0	6																		
D	-2	-2	1	6																	
С	0	-3	-3	-3	9																
Q	-1	1	0	0	-3	5															
E	-1	0	0	2	-4	2	5														
G	0	-2	0	-1	-3	-2	-2	6													
Η	-2	0	1	-1	-3	0	0	-2	8												
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4											
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4										
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5									
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5								
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6							
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7						
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4					
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5				
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11			
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7		
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4	
Х	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1

V	P	N	M
V	P		
	P	N	

VP IP LP MP
PN PD

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

	A	R	N	D	C	Q	E	G	Н	I	L	K	М	F	P	S	T	W	Y	V	X
A	4																				
R	-1	5																			
N	-2	0	6																		
D	-2	-2	1	6																	
С	0	-3	-3	-3	9																
Q	-1	1	0	0	-3	5															
E	-1	0	0	2	-4	2	5														
G	0	-2	0	-1	-3	-2	-2	6													
Η	-2	0	1	-1	-3	0	0	-2	8												
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4											
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4										
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5									
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5								
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6							
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7						
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4					
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5				
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11			
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7		
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4	
Х	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1

V	P	N	M
V	P		
	P	N	

VP IP LP MP
PN PD PH

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

	Α	R	N	D	C	Q	E	G	Н	I	L	K	М	F	P	S	T	W	Y	V	X
Α	4																				
R	-1	5																			
N	-2	0	6																		
D	-2	-2	1	6																	
С	0	-3	-3	-3	9																
Q	-1	1	0	0	-3	5															
E	-1	0	0	2	-4	2	5														
G	0	-2		-1	-3	-2	-2	6													
Η	-2	0	1	-1	-3	0	0	-2	8												
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4											
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4										
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5									
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5								
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6							
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7						
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4					
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5				
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11			
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7		
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4	
Х	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1

V	P	N	M
V	P		
	P	N	

VP	IP	LP	MP
PN	PD	PH	PS

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

	A	R	N	D	С	Q	E	G	Н	I	L	K	Μ	F	P	S	T	W	Y	V	X
Α	4																				
R	-1	5																			
N	-2	0	6																		
D		-2	1	6																	
C	0	-3	-3	-3	9																
Q	-1	1	0	0	-3	5															
E	-1	0	0	2	-4	2	5														
G	0	-2		-1	-3	-2	-2	6													
Η	-2	0	1	-1	-3	0	0	-2	8												
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4											
L		-2		-4	-1	-2	-3	-4	-3	2	4										
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5									
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5								
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6							
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7						
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4					
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5				
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11			
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7		
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4	
Χ	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1

V	P	N	M
V	P		
	P	N	
		N	M

VP	IP	LP	MP
PN	PD	PH	PS

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

	A	R	N	D	C	Q	E	G	Н	Ι	L	K	M	F	P	S	T	M	Y	V	X
Α	4																				
R	-1	5																			
N	-2	0	6																		
D	-2	-2	1	6																	
C	0	-3	-3	-3	9																
Q	-1	1	0	0	-3	5															
E	-1	0	0	2	-4	2	5														
G	0	-2	0	-1	-3	-2	-2	6													
H	-2	0	1	-1	-3	0	0	-2	8												
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4											
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4										
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5									
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5								
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6							
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7						
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4					
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5				
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11			
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7		
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4	
Χ	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1

V	P	N	M
V	P		
	P	N	
		N	M

VP	IP	LP	MP
PN	PD	PH	PS

NM

Given the sequence **VPNM**, a threshold of 8, and *k*-mer size 2 perform BLAST preprocessing to find the set of *k*-mers to search for.

	A	R	N	D	C	Q	E	G	H	I	L	K	M	F	P	S	T	M	Y	V	X	
A	4																					
R	-1	5																				
N	-2	0	6																			
D	-2	-2	1	6																		
С	0	-3	-3	-3	9																	
Q	-1	1	0	0	-3	5																
E	-1	0	0	2	-4	2	5															
G	0	-2	0	-1	-3	-2	-2	6														
H	-2	0	1	-1	-3	0	0	-2	8													
I	-1	-3	-3	-3	-1	-3	-3	-4														
L				-4	-1	-2	-3	-4	-3	2	4											
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5										
Μ	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5									
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6								
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7							
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4						
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5					
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11				
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7			
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4		
Х	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	

V	P	N	M
V	P		
	P	N	
		N	M

VP	IP	LP	MP
PN	PD	PH	PS

NL

NM

Lets BLAST some stuff!

https://blast.ncbi.nlm.nih.gov/Blast.cgi